

RATIO, RATE AND PROPORTION - IGCSE

You must write down all the stages in your working.

Q1

Pieter owns a currency conversion shop.

Last Monday, Pieter changed a total of 20 160 rand into a number of different currencies.

He changed $\frac{3}{10}$ of the 20 160 rand into euros. $\frac{3}{10} \times 20\ 160 = 2016$ rands ①

He changed the rest of the rands into dollars, rupees and francs in the ratios 9:5:2

Pieter changed more rands into dollars than he changed into francs.

Work out how many more.

$$\text{Remaining Rands} = 18\ 144$$

$$\begin{aligned} 1 \text{ part} &= 18\ 144 \div 16 \\ &= 1134 \end{aligned} \quad \text{①}$$

$$\begin{aligned} \text{Rands changed to Dollar} &= 9 \times 1134 = 10\ 206 \\ \text{Rands changed to Francs} &= 2 \times 1134 = \underline{2\ 268} \end{aligned} \quad \left. \vphantom{\begin{aligned} \text{Rands changed to Dollar} \\ \text{Rands changed to Francs} \end{aligned}} \right\} \text{①}$$

$$\text{Difference} = \underline{\underline{7\ 938}} \text{ rands} \quad \text{①}$$


..... rand (4)

Q2

Danil, Gabriel and Hadley share some money in the ratios 3:5:9

The difference between the amount of money that Gabriel receives and the amount of money that Hadley receives is 196 euros.

Work out the amount of money that Danil receives.

$$\begin{array}{l} D : G : H \\ 3 \quad 5 \quad 9 \end{array} \quad \left| \quad \begin{array}{l} 4 \text{ parts} = 196 \\ 1 \text{ part} = 49 \end{array} \right.$$


$$\begin{aligned} \text{Danil} &= 49 \times 3 \\ &= 147 \end{aligned}$$

147

..... euros

Q3

In a box, there are only green sweets, orange sweets and yellow sweets.

There are 280 sweets in the box so that

the number of green sweets : the number of orange sweets = 2 : 3

and

the number of orange sweets : the number of yellow sweets = 1 : 5

Work out how many green sweets there are in the box.

$$\begin{array}{r} G : O : Y \\ 2 \quad 3 \\ \quad 1 \quad 5 \end{array} \times 3$$

$$= \quad 2 \quad 3 \quad 15$$

$$\begin{aligned} 1 \text{ part} &= 280 \div 20 \\ &= 14 \end{aligned}$$

$$\begin{aligned} \text{Number of Green sweets} &= 14 \times 2 \\ &= \underline{28} \end{aligned}$$

(3)

Q4

Eli and Peta share \$275 in the ratio 2:3

Eli gives $\frac{3}{11}$ of his share to charity.

Peta gives 0.32 of her share to charity.

Work out the total amount that Eli and Peta give to charity.

$$1 \text{ part} = 275 \div 5 \\ = 55 \quad (1)$$

$$\text{Eli} = 2 \times 55 \\ = 110$$

$$\text{Peta} = 3 \times 55 \\ = 165 \quad (1)$$

Money to Charity

$$\text{Eli: } \frac{3}{11} \times 110 \\ = 30$$

$$\text{Peta} = 0.32 \times 165 \\ = 52.8 \quad (1)$$

\$ 52.8 (1)

$$\text{Total} = 30 + 52.8 \\ = 82.8$$

(4)

The people working for a company work in Team A or in Team B.

number of people in Team A: number of people in Team B = 3:4

$\frac{4}{5}$ of Team A work full time.

24% of Team B work full time.

Work out what fraction of the people working for the company work full time.
Give your fraction in its simplest form.

$$A \text{ full time} = \frac{4}{5} \times \frac{3}{7} = \frac{12}{35}$$

$$B \text{ full time} = 0.24 \times \frac{4}{7} = \frac{24}{175}$$

$$\begin{aligned} \text{Full time} &= \frac{12}{35} + \frac{24}{175} \\ &= \frac{12}{25} \end{aligned}$$

(4)

Q6

Work out the difference between the largest share and the smallest share when 3450 yen is divided in the ratios 2:6:7

$$\begin{aligned} 1 \text{ part} &= 3450 \div 15 \\ &= 230 \end{aligned}$$

$$\begin{aligned} \text{Largest} &= 230 \times 7 \\ &= 1610 \end{aligned}$$

$$\begin{aligned} \text{Smallest} &= 230 \times 2 \\ &= 460 \end{aligned}$$

$$\begin{aligned} \text{Difference} &= 1610 - 460 \\ &= 1150 \end{aligned}$$

1150

..... yen

Q7

Pau, Sam and Tia share £240 in the ratios 3:4:5

Sam and Tia each give £10 of their share to Pau.

Work out the ratios of the amounts of money that Pau, Sam and Tia now have.

Give your answer in its simplest form.

$$1 \text{ part} = 240 \div 12 = 20$$

$$\begin{aligned} \text{Pau} &= 20 \times 3 \\ &= 60 \end{aligned}$$

$$\begin{aligned} \text{Sam} &= 20 \times 4 \\ &= 80 \end{aligned}$$

$$\begin{aligned} \text{Tia} &= 20 \times 5 \\ &= 100 \end{aligned}$$

$$\text{New Ratio} = P : S : T$$

$$80 : 70 : 90$$

8 : 7 : 9

..... (4)

Q8

Avril bakes a cake.

She uses flour, butter and sugar such that

$$\begin{aligned}\text{weight of flour : weight of butter} &= 6 : 5 \\ \text{weight of butter : weight of sugar} &= 3 : 2\end{aligned}$$

Avril uses 120 grams of sugar.

Work out the weight of flour Avril uses.

$$\begin{array}{r|l} F : B : S & \\ 6 & 5 & & \times 3 \\ & 3 & : 2 & \times 5 \\ \hline 18 & 15 & : 10 & \end{array}$$

$$\begin{aligned}1 \text{ part} &= 120 \div 10 \\ (4) &= 12\end{aligned}$$

$$\begin{aligned}\text{Flour used} &= 18 \times 12 \\ &= 216\text{g}\end{aligned}$$

Ishir plants 600 bulbs in a garden.

He plants tulip bulbs, crocus bulbs and daffodil bulbs so that

number of tulip bulbs : number of crocus bulbs : number of daffodil bulbs = 9 : 4 : 2

45% of the tulip bulbs are for yellow flowers.

$\frac{5}{8}$ of the crocus bulbs are for yellow flowers.

All of the daffodil bulbs are for yellow flowers.

Work out the number of bulbs that are for yellow flowers.

$$\begin{aligned} 1 \text{ part} &= \frac{600}{15} \\ &= 40 \end{aligned}$$

$$\text{Tulip} = 9 \times 40 = 360$$

$$\text{Crocus} = 4 \times 40 = 160$$

$$\text{Daffodil} = 2 \times 40 = 80$$

$$\text{Yellow Tulip} = 0.45 \times 360 = 162$$

$$\text{Yellow Crocus} = \frac{5}{8} \times 160 = 100$$

$$\begin{aligned} \text{Yellow flowers} &= 162 + 100 + 80 \\ &= \underline{\underline{342}} \end{aligned}$$

.....(5)